

# Computer-assisted Trajectory Planning for Percutaneous Needle Insertions

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## Short title

Trajectory Planning for Needle Insertions

# Computer-assisted Trajectory Planning for Percutaneous Needle Insertions

## Abstract

**Purpose:** Computed tomography (CT) guided minimally invasive interventions such as biopsies or ablation therapies often involve insertion of a needle-shaped instrument into the target organ (e.g. the liver). Today, these interventions still require manual planning of a suitable trajectory to the target (e.g. the tumor) based on the slice data provided by the imaging modality. However, taking into account critical structures and other parameters crucial to the success of the intervention - such as instrument shape and penetration angle - is challenging and requires a lot of experience.

**Methods:** To overcome these problems, we present a system for the automatic or semi-automatic planning of optimal trajectories to a target, based on 3D reconstructions of all relevant structures. The system determines possible insertion zones based on so-called *hard constraints* and rates the quality of these zones by so-called *soft constraints*. The concept of *pareto optimality* is utilized to allow for a weight-independent proposal of insertion trajectories. In order to demonstrate the benefits of our method, automatic trajectory planning was applied retrospectively to n=10 data sets from interventions in which complications occurred.

**Results:** The efficient (graphics processing unit-based) implementation of the constraints results in a mean overall planning time of about 9 seconds. The examined trajectories, originally chosen by the physician, have been rated as follows: in six cases, the insertion point was labeled invalid by the planning system. For two cases, the system would have proposed points with a better rating according to the *soft constraints*. For the remaining two cases the system would have indicated poor rating with respect to one of the *soft constraints*. The paths proposed by our system were rated feasible and qualitatively good by experienced interventional radiologists.

**Conclusions:** The proposed computer-assisted trajectory planning system is able to detect unsafe and propose safe insertion trajectories and may especially be helpful for interventional radiologist at the beginning or during their interventional training.

27 **Key Words:** interventional radiology, trajectory planning, radiofrequency ablation, image-guided  
28 therapy, computer-aided intervention

## 29 **1 Introduction**

30 Image-guided minimally-invasive interventions are gaining in importance in clinical routine today.  
31 Thermal ablation therapies, for example, are increasingly applied for treatment of focal malignant  
32 diseases. For 20% of all malignancies in the liver, surgical resection cannot be used for treatment,  
33 and radiofrequency ablation (RFA) emerged as a favored alternative [1]. This procedure requires  
34 insertion of a needle-shaped instrument into the cancerous tissue and therefore relies on precise  
35 planning of an appropriate insertion trajectory. Although protocols for manual trajectory planning  
36 are well established in clinical routine, the lack of three-dimensional (3D) presentation of the medical  
37 imaging data may lead to complications. Because the planning is mostly done on slice-based  
38 reformations of the 3D volume, the shape and length of the instrument can only be considered  
39 roughly and the penetration angle of the instrument is difficult to determine as well.

40 Several approaches to automatic trajectory planning have been presented in the context of  
41 neurosurgery. Although structures in the brain can be considered more rigid compared to abdominal  
42 organs, the process of planning a straight trajectory is similar for both body parts. The early work of  
43 Vaillant *et al.* [2] presents an algorithm that allows for automatically computing a rating of possible  
44 insertion points considering critical structures in the brain. The basic idea is to minimize a cost  
45 function over all possible paths that sums up individual, manually assigned voxel costs that take into  
46 account the critical structures. Brunenberg *et al.* [3] and Shamir *et al.* [4] [5] pointed out that this  
47 cumulative risk computation can be misleading and introduced the concept of risk volume, where  
48 each voxel is assigned a risk value dependent on the minimal distance to the surrounding critical  
49 structures. Thus, the manual assignment of cost values can be replaced by an efficient computation  
50 on distance maps. Shamir *et al.* also presented a quantitative clinical evaluation that showed  
51 improvements in procedure time and trajectory risk. Although these methods are quite efficient  
52 when considering the proximity of the trajectory to critical structures, it may be difficult to integrate

53 other restrictions to the path which are of interest for interventions in the abdomen such as insertion  
54 angle or instrument shape. Navkar *et al.* [6] presented an approach based on projections of the  
55 critical structures on the head surface. They are thus able to detect trajectories which would hit or  
56 are too close to a critical structure and can also consider the length of the trajectories in their  
57 planning visualization. Nevertheless, they did not quantitatively evaluate their method on clinical  
58 data. Recently, Essert *et al.* [7] presented a method for automatic computation of electrodes  
59 trajectory for deep brain stimulation. Possible trajectories are determined by solving a set of  
60 geometric constraints. In a retrospective study on four patients, they could show the applicability of  
61 their method.

62 Automatic and semi-automatic approaches to trajectory planning in the abdomen are sparse. Most  
63 methods concentrate on calculation and simulation of the ablation zone and the resulting optimal  
64 probe placement with respect to the coverage of the tumor. Altrogge *et al.* [8] present a finite  
65 elements (FEM)-based approach for optimizing the needle placement taking into account the electric  
66 potential of the probe and the steady state of the heat distribution during RF ablation. The authors  
67 also present an integration of this optimization module into a workflow oriented software module  
68 (Weihsen *et al.* [9]). This includes tools for interactively planning the trajectory by defining the  
69 center of the necrosis zone and the position of the shaft of the needle in the CT slices. Butz *et al.* [10]  
70 also focus on optimizing the insertion trajectory with respect to the necrosis zone. Additionally, they  
71 use some basic three-dimensional visualization of the planned trajectory and the surrounding organs,  
72 allowing the physician to optimize the planning result. Zhai *et al.* [11] propose a framework for  
73 calculating a 3D visualization of the complete surgery scene including the trajectory and a 3D model  
74 of the necrosis zone. Starting from an interactively chosen insertion trajectory, the necrosis model is  
75 computed taking into account the microwave energy, the tissue temperature and the blood  
76 perfusion rate. Planning of the actual trajectory considering e.g. critical structures and an automatic  
77 rating of the chosen insertion point are not part of these methods.

78 Villard<sup>[12],[13],[14]</sup> and Baegert [15],[16],[17] propose a method based on a constraint concept for  
79 automatically computing insertion trajectories. An insertion trajectory consists of the given target  
80 point and an insertion point on the skin. So-called *hard constraints* are used to determine the  
81 insertion zones on the skin, which represent trajectories to the target that do not violate any  
82 restrictions to the path such as hitting a critical structure or exceeding the needle length. The quality  
83 of the trajectories that are allowed according to the *hard constraints* is then rated by so-called *soft*  
84 *constraints* that represent clinically relevant parameters such as the distance to critical structures.  
85 Several *soft constraints* can be combined using a weighted sum in order to obtain an overall rating of  
86 a given trajectory. Note that, as pointed out by Brunenberg *et al.* or Shamir *et al.*, weighted sum  
87 rating may be misleading. If a trajectory e.g. passes close to a critical structure but is also very short,  
88 the rating of the constraint considering the proximity to critical structures would be poor whereas  
89 the rating of the constraint considering the length would be good. Averaging these ratings could  
90 result in choosing this trajectory and a potential complication at the critical structure. Because all  
91 calculations are based on surface representations of the tumor, the liver, the skin and the critical  
92 structures, the proposed algorithms are still time consuming and require optimization. Using the  
93 concept of risk volume [5] could be an interesting alternative. Furthermore, a clinical evaluation  
94 showing the suitability of the proposed systems for interventions in the abdomen has not yet been  
95 conducted.

96 Recently, another planning approach has been proposed by Schumann *et al.* [18] where, as in Villard  
97 and Baegert, a set of constraints is used to determine suitable insertion trajectories. The authors use  
98 a method independent of the mesh representation of the critical structures by generating so-called  
99 *constraint maps* for each restriction by computing a cylindrical projection with the center at the  
100 target point. Each *constraint map* is rated by a constraint-specific rating function and merged to a  
101 weighted combination of all constraints. The maxima in this combined map correspond to the  
102 possible insertion trajectories. The authors report a total computation time of 6 seconds for  
103 determining optimal insertion trajectories on a standard computer. However, the weight factors of

104 each constraint still must be set manually and an evaluation showing the clinical suitability of the  
105 proposed trajectory planning system has not yet been performed.

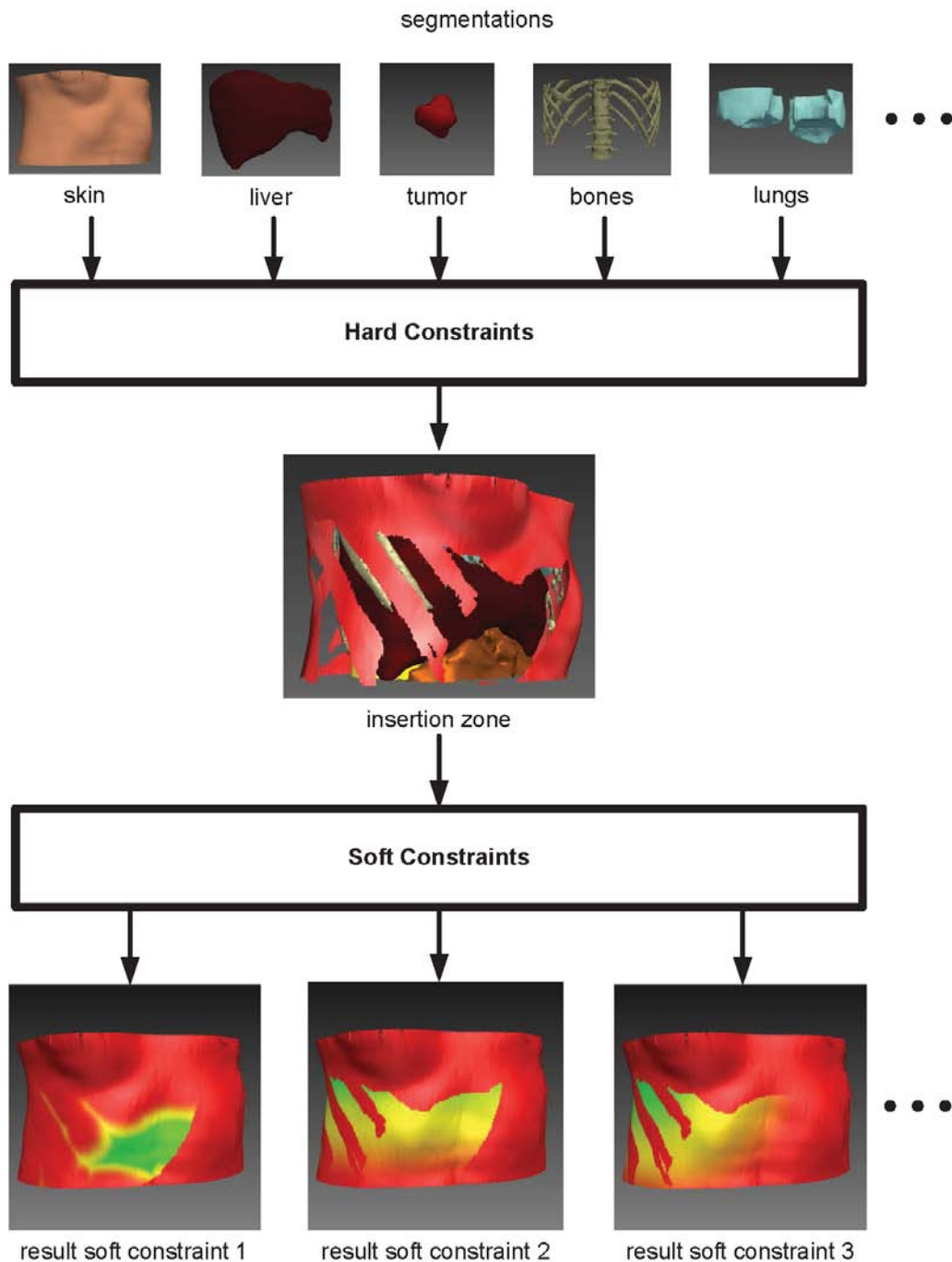
106 The main contribution of this work is two-fold. Firstly, we use the concept of *pareto optimality* which  
107 allows rating the trajectories weight-independently. Secondly, we evaluate an advanced version of  
108 the constraint concept for automatic trajectory planning retrospectively on a set of 10 clinical cases,  
109 in which complications occurred, to demonstrate the performance and clinical suitability of the  
110 proposed approach. The planning system aims to be helpful especially for unexperienced  
111 interventional radiologists and in difficult cases where e.g. the target is located close to a critical  
112 structure such as the heart.

113 The remaining part of this paper is organized as follows: First, we describe how the concept of *hard*  
114 *constraints* (section 2.1) and *soft constraints* (section 2.2) is realized. Then we concentrate on how to  
115 automatically select the best- suited trajectories using the concept of *pareto optimality* (section 2.3,  
116 2.4). The design of the retrospective clinical study is presented in section 2.5. Finally, the results of  
117 the study are shown in section 3 and discussed in section 4.

## 118 **2 Materials and Methods**

119 We extend the work of Villard [14] and Baegert [15] to achieve a fast, robust, and extendable  
120 implementation for the automated trajectory planning. Although the main focus is on interventions  
121 in the liver, the system should be easy to adapt for usage in other body parts. Thus, a modular  
122 structure should allow integration of new constraints needed for different interventions. Also, the  
123 choice of the critical structures is not limited to a particular set but is entirely up to the interventional  
124 radiologist. In most cases of RFA liver interventions, bones, lungs, heart, stomach, gall bladder and  
125 big vessels are considered for planning. All components of the system have been developed within  
126 the Medical Imaging Interaction Toolkit (MITK) [19], a convenient platform for developing medical  
127 image processing applications, providing functionality similar to that of commercial image guided  
128 therapy systems. The computations for the planning result rely on mesh representations of the

129 segmentations of skin, liver, tumor and critical structures which can be achieved with any  
 130 segmentation tool. For this study, we used the semi-automatic, interactive approach presented by  
 131 Maleike *et al.* [20].



132 **Figure 1.** Constraint concept of the automatic trajectory planning. Surfaces of the skin, the liver, the  
 133 tumor and other critical structures are created from corresponding segmentations. The insertion  
 134 zone on the skin is determined using a combination of *hard constraints*. The points of the skin where  
 135 insertion of the needle is not applicable are marked in red. A rating of those insertion zones is  
 136 achieved by applying a combination of *soft constraints*.

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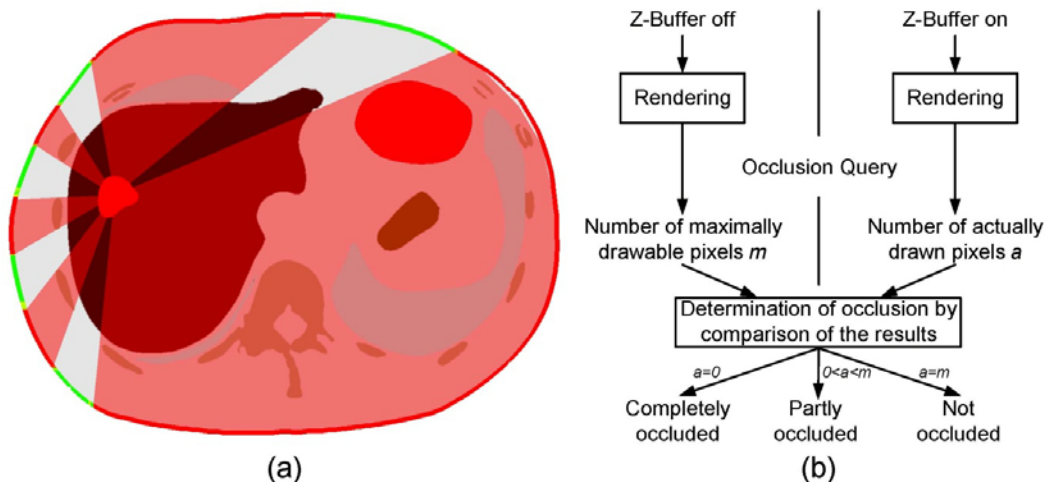
138 The general optimization and extension of the constraint concept is described in section 2.1 and 2.2.  
 139 The primary focus of this paper is on an additional, pareto-based planning interface for the physician  
 140 (section 2.3) and a retrospective clinical study for quality assessment of the method (section 2.5).

## 141 2.1 Determination of insertion zones (*hard constraints*)

142 The points of the skin are progressively eliminated from the possible insertion zone by applying  
 143 different *hard constraints* in a pipeline if the corresponding trajectory to the target does not satisfy  
 144 the condition of the constraints (e.g. a maximum length of the trajectory) and thus would cause  
 145 major complications during intervention. Each point in the resulting insertion zone (Figure 1) then  
 146 defines a trajectory together with the predefined target point. Five different *hard constraints* have  
 147 been implemented and used for this study and will be described in detail in the following paragraphs.

### 148 Occlusion Constraint

149 The *occlusion constraint* is used to determine those parts of the skin for which the corresponding  
 150 insertion trajectory would not traverse any critical structure.



151 **Figure 2.** (a) Schematic illustration of the *occlusion constraint* and the determination of the insertion  
 152 zone. All points of the skin that are visible from the target point are marked as possible insertion  
 153 points. (b) Implementation of the *occlusion constraint* using fast occlusion queries. In a first rendering  
 154 step with the Z-buffer turned off, the occlusion query returns the maximal number of drawable pixels  
 155 for every triangle of the mesh of the skin ( $m$ ). For the second rendering with the Z-buffer turned on,  
 156 the occlusion query returns the number of actually visible pixels ( $a$ ). The difference between these  
 157 two values determines whether the triangle is completely visible ( $a = m$ ), partly visible ( $0 < a < m$ ) or  
 158 not visible ( $a = 0$ ).  
 159



160 The task of finding those points can be modeled as a line-of-sight problem, in which the virtual  
161 camera, which is used during the rendering<sup>1</sup>, is placed at the target position. All points of the skin  
162 that are visible from this position - and thus not occluded by any critical structure - are marked as  
163 possible insertion points (Figure 2a). To allow for an efficient computation of these insertion zones,  
164 the so-called occlusion queries are used (Figure 2b). Every triangle of the mesh representing the skin  
165 is drawn (rendered) twice. In the first step with the Z-buffer<sup>2</sup> turned off, the maximal number  $m$  of  
166 drawable pixels is determined for each triangle. In the second run with the Z-buffer turned on, the  
167 number of actually visible pixels  $a$  of this triangle is returned. These numbers indicate whether the  
168 triangle is completely visible ( $a = m$ ), partly occluded ( $0 < a < m$ ) or not visible ( $a = 0$ ).

169 This approach already uses the potential of modern graphics hardware, but still shows a performance  
170 leak as the central processing unit (CPU) and the graphics-processing unit (GPU) is not working  
171 parallel when a whole mesh is examined. The CPU has to wait for the GPU while the rendering of a  
172 triangle is in progress, and the GPU has to wait for the CPU, while the latter evaluates the result of  
173 the occlusion query. To overcome this problem, we introduced a buffer of occlusion queries, which  
174 will be extended as long as all triangles are rendered. The CPU in parallel reads the results of the  
175 completed queries from the buffer and processes it. This ensures a maximal utilization of resources.

## 176 **Safety Margin around Target Constraint**

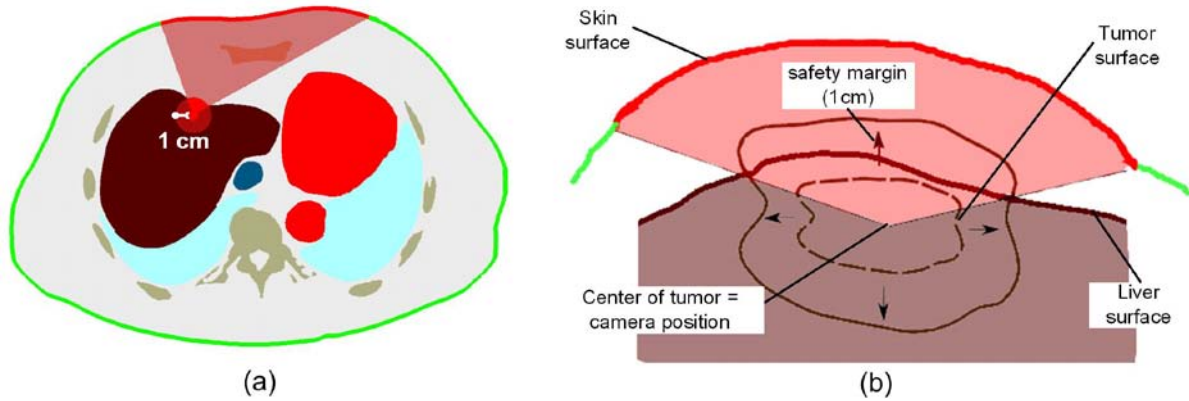
177 The *safety margin around target constraint* ensures that a safety margin of at least 1 cm of healthy  
178 liver tissue is provided on that part of the trajectory located between the surface of the tumor and  
179 the liver capsule. This is needed to prevent bleeding and to allow cauterization and thus minimize the  
180 possible spreading of tumor cells. [21] Technically, this constraint marks parts of the liver surface as  
181 additional critical structures internally using the *occlusion constraint* as shown in Figure 3. Those  
182 critical structures are then considered by the “global” *occlusion constraint*.

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<sup>1</sup> **Rendering:** Process of generating an image of a scene (e.g. three-dimensional representation of different organs) from an underlying model (e.g. surface representation) of that scene

<sup>2</sup> **Z-Buffer:** Array of depth values of pixels generated during the rendering process. If two objects of the scene would be rendered into the same pixel, Z-buffering chooses the one closer to the camera.

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**Figure 3.** (a) Schematic illustration of the *safety margin around target constraint*, which ensures a safety margin of healthy liver tissue of 1cm on that part of the trajectory located between the surface of the tumor and the liver capsule. (b) Computation of additional critical structures for the *occlusion constraint*. First the tumor (dashed line) is dilated by the safety margin. Then the *occlusion constraint* is internally used to determine those parts of the liver that are visible from the center of the tumor. These represent the points which would result in a trajectory that does not cover the safety margin between the tumor surface and the liver capsule. Finally, these parts of the liver are defined as additional critical structures to be used by the *occlusion constraint*.

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### Tangency Constraint

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The *tangency constraint* ensures that the angle in which the trajectory intersects the liver surface is bigger than  $20^\circ$  and therefore prevents the needle from slipping off the liver surface (Figure 4a). To allow for an efficient computation of the corresponding insertion zones, all triangles of the liver surface are determined for which the trajectory would show an insertion angle to the liver surface smaller than  $20^\circ$ . These triangles are then used as additional critical structures for the *occlusion constraint*.

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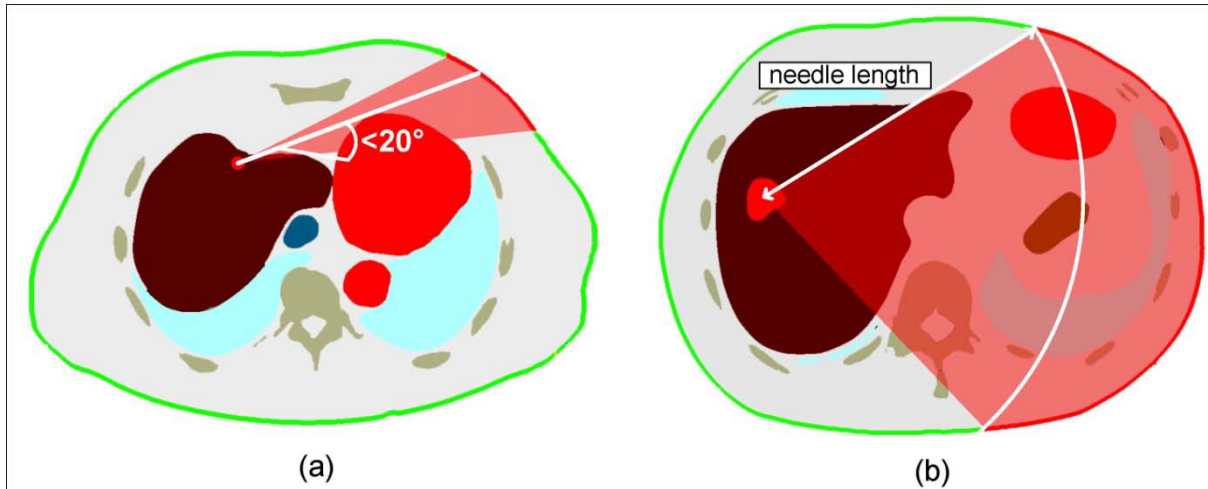
202

### Needle Length Constraint

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The *needle length constraint* ensures that the trajectory is shorter than the needle to be inserted. All insertion points leading to a longer trajectory are eliminated from the insertion zone (Figure 4b).



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 206 **Figure 4.** (a) Schematic illustration of the *tangency constraint*, which ensures that the angle in which  
 207 the trajectory intersects the liver surface is bigger than  $20^\circ$ . (b) The *needle length constraint* excludes  
 208 all insertion trajectories from the insertion zone that are longer than the needle.

### 209 **RFA-Umbrella Constraint**

210 Radiofrequency ablations are generally performed using a needle-shaped applicator. In order to  
 211 enlarge the necrosis zone when treating large tumors, recent needle models offer the possibility to  
 212 deploy a set of spikes that form a kind of umbrella. Common models currently used in clinical routine  
 213 are the LeVeen® Electrode System and the Starburst™ Talon Device. Their deployed spikes can be  
 214 represented by parts of a superquadric toroid which can be mathematically modeled using implicit  
 215 functions that allow for fast and flexible computation of intersections with critical structures. In  
 216 general, implicit functions are functions in which the dependent variable has not been given explicitly  
 217 but as the solution of the equation  $F(x, y, z) = 0$ . They can be used for the mathematical description  
 218 of a surface representation of an object [22]. Evaluating the so-called inside-out function  $F(x, y, z)$   
 219 allows to decide whether the corresponding point  $(x, y, z)$  lies inside ( $F(x, y, z) < 0$ ), outside  
 220 ( $F(x, y, z) > 0$ ) or on the surface ( $F(x, y, z) = 0$ ).

221 The *RFA-umbrella constraint* ensures that this additional umbrella does not hit any critical structure

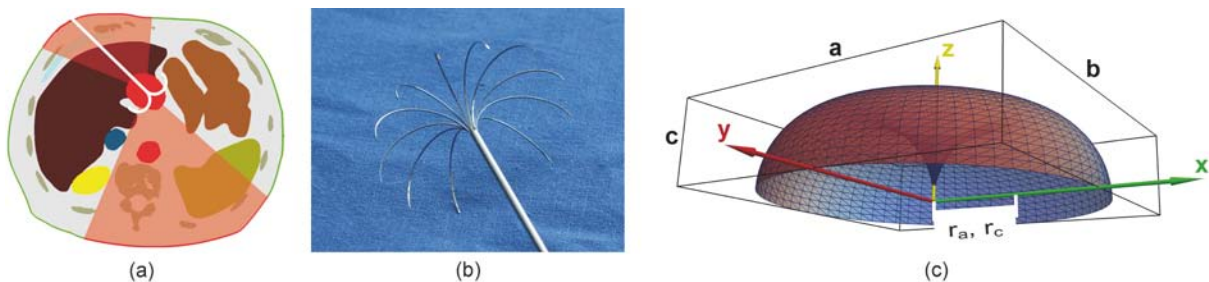
222 (Figure 5). The inside-out function is defined by a superquadric toroid  $T(x, y, z) = (r_c -$

223  $\sqrt{x^2 + y^2})^2 + z^2 - r_a^2$ , where  $r_c$  is the radius from the center of the torus to the center of the torus

224 tube and  $r_a$  is the radius of the torus cut by the six planes that form a box with the extents  $a, b$ , and  $c$

225 (Figure 5c). For every insertion trajectory and the corresponding orientation of the umbrella, the

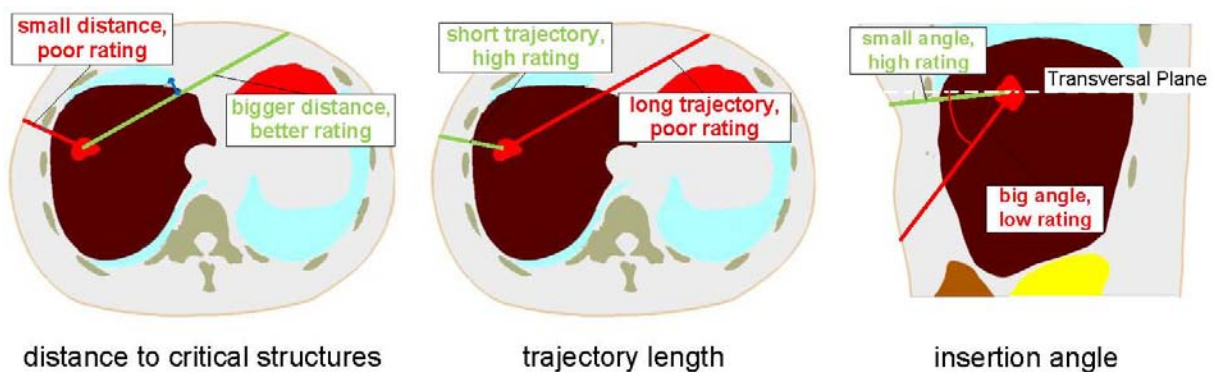
226 resulting implicit function is evaluated for every point of the surface of the critical structures. If one  
 227 of the resulting values is smaller than 0, the corresponding insertion point on the skin is eliminated  
 228 from the insertion zone. Note that if no surface point is located inside the umbrella model, the  
 229 umbrella is located completely outside or inside of a critical structure. The inside case, which would  
 230 cause complications that could not be detected by this constraint, is not possible because the target  
 231 would also have to lie inside the critical structure.



232  
 233 **Figure 5.** (a) Schematic illustration of the *RFA-umbrella constraint* that ensures the umbrella- shaped  
 234 electrode of the RFA needle does not hit any critical structures. (b) Prong umbrella of LeVein®  
 235 Electrode System. (c) Surface representation using implicit function.

## 236 2.2 Rating of insertion zones (*soft constraints*)

237 The previously determined insertion zones are rated by three different *soft constraints* defined by a  
 238 corresponding cost function, each representing one clinically relevant parameter (Figure 6). All *soft*  
 239 *constraints* are normalized to allow for a weighted combination as reported by Villard/Baegert [17].  
 240 The rating value of the *soft constraints* is between 0 and 1, where 0 refers to an invalid trajectory and  
 241 1 refers to a trajectory that is considered relatively safe.



242 distance to critical structures trajectory length insertion angle  
 243 **Figure 6.** Rating of the insertion zones by the *soft constraints*: The *distance to critical structures*  
 244 *constraint* rates the possible insertion trajectories according to their distance to critical structures.  
 245 The length of the trajectory is considered by the *trajectory length constraint*. The insertion angle  
 246 *constraint* prefers trajectories that have a small angle to the axial slice the target lies in.

247 **Distance to critical structures constraint**

248 The *distance to critical structures constraint* (DTCS)  $c_1$  rates the possible insertion trajectory  $tr$   
249 according to its distance  $d(tr)$  to critical structures, which is defined as the shortest distance  
250 between the insertion trajectory and any mesh point of the critical structures. The bigger the  
251 distance is, the better the trajectory is rated. To reduce computation time, the mesh points of all  
252 critical structures are initially stored in so-called KD-trees [23] which represent a data structure that  
253 allows for high performance navigation in a large set of points. The rating is computed as follows:

$$r_{c_1}(tr) = \frac{d(tr) - d_{min}}{d_{max} - d_{min}}$$

254 where  $d_{min}$  and  $d_{max}$  are the minimal and maximal distance to critical structures, respectively.

255 **Trajectory length constraint**

256 The trajectory length  $l(tr)$  is considered by the *trajectory length constraint* (TL)  $c_2$ . The shorter the  
257 trajectory, the better the corresponding insertion point is rated with the rating being proportional to  
258 the trajectory length. The rating is computed as follows:

$$r_{c_2}(tr) = 1 - \frac{l(tr) - l_{min}}{l_{max} - l_{min}}$$

259 where  $l_{min}$  and  $l_{max}$  are the minimal and maximal trajectory length, respectively.

260 **Insertion angle constraint**

261 Physicians often tend to insert the needle in the axial slice as acquired by the CT (in-plane).

262 Therefore, the *insertion angle constraint* (IA)  $c_3$  rates those trajectories better that are closer to the  
263 axial plane the target is in. It thus reduces the number of degrees of freedom which have to be  
264 considered when transferring the plan to the patient. Furthermore, the trajectory can be confirmed  
265 more easily in a control CT scan. The rating is calculated from the insertion angle  $\alpha(tr)$  according to  
266 an exponential scoring function, which was determined empirically:

$$r_{c_3}(tr) = \begin{cases} e^{-\frac{\alpha(tr)^2}{20^{\circ 2}}}; & \alpha(tr) \leq 40^{\circ} \\ 0 & ; \alpha(tr) > 40^{\circ} \end{cases}$$

## 267 **2.3 Semi-automatic selection of a trajectory**

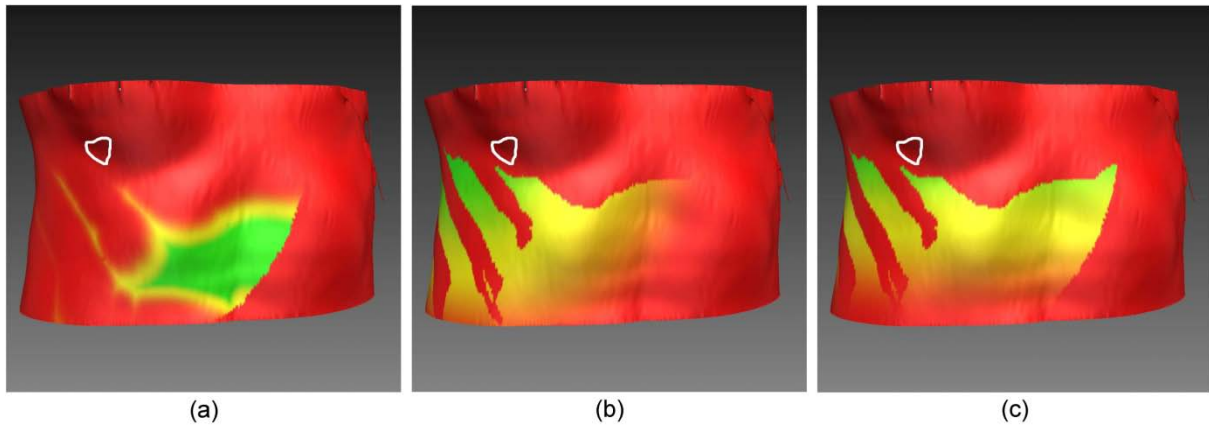
268 Given the insertion zones, there are now many candidates for an insertion point of the trajectory. To  
 269 decide on the final path, the control is returned to the radiologist who chooses the one he personally  
 270 rates best. To support him with this decision, we developed two alternatives to assist planning of the  
 271 final insertion trajectory. Firstly, as proposed by Baegert *et al.* [15], a proposal for suitable insertion  
 272 trajectories can be achieved by adapting the weights of the *soft constraints* (section 2.3.1). Secondly,  
 273 the principle of *pareto optimality* can be used for a weight-independent proposal of appropriate  
 274 insertion trajectories (section 2.3.2).

### 275 **2.3.1 Weight-based trajectory planning**

276 To achieve a rating of the insertion zones, the normalized result  $r_{c_i}(tr)$  of each soft constraint is  
 277 considered in a weighted sum.

$$R(tr) = \sum_{i=1}^n w_i r_{c_i}(tr)$$

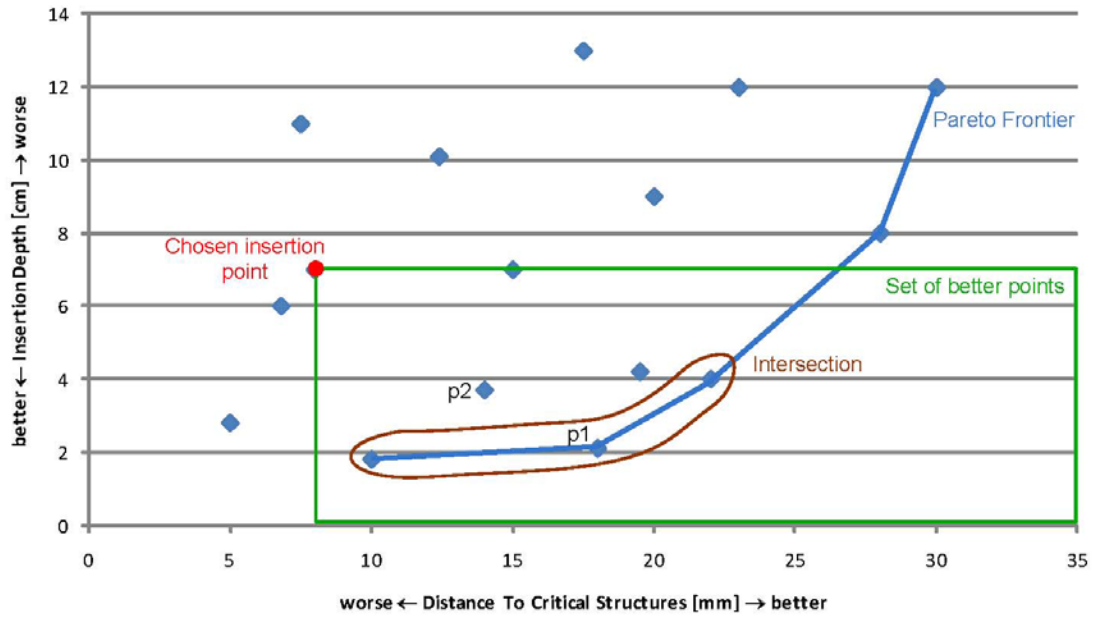
278 The individual weighting factors  $w_i$  are manually selected with  $\sum_{i=1}^n w_i = 1$ . The resulting rating  $R$  is  
 279 visualized in the insertion zone using a color gradient ranging from green ("good rating", big  $R$ ) to red  
 280 ("poor rating", small  $R$ ). An update of the weights leads to a change of the color gradient (Figure 7).  
 281 For planning the final insertion trajectory, the insertion point can simply be marked by clicking on the  
 282 desired location on the skin. As an extension of the work of Villard and Baegert, a set of better points  
 283 (at least better in one parameter and not worse in another one) can be shown (Figure 8 and 9b).



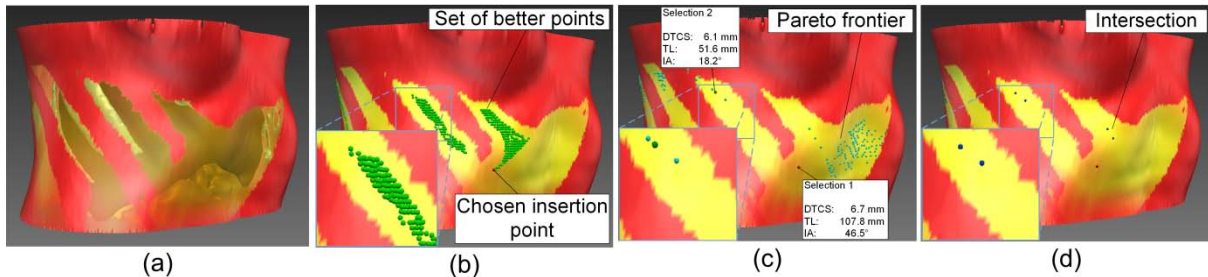
284  
 285 **Figure 7.** Color coded insertion zones for differently weighted combinations of the *soft constraints*  
 286 based on the same combination of *hard constraints*. 100% means that the weight was 1 for the  
 287 examined constraint and 0 for the other constraints. The contour of the tumor is drawn in white. (a)  
 288 100% distance to critical structures. (b) 100% insertion depth. (c) 100% in-plane.  
 289

### 290 **2.3.2 Pareto-based trajectory planning**

291 To provide an automatic way of planning a trajectory, the principle of *pareto optimality* [24] is used  
 292 to determine suitable insertion trajectories without the need of weights (Figure 8). A point in a set of  
 293 points is called *pareto-optimal* if there is no other point in this set that scores better in one  
 294 parameter without scoring worse in another one. The set of all *pareto-optimal* points is called *pareto*  
 295 *frontier*. In our case, the parameter space is spanned by the individual *soft constraints*. Applying the  
 296 pareto-based optimization, the system can either show all *pareto-optimal* points as a proposal for  
 297 trajectories or the intersection between this *pareto frontier* and the set of better points (cf. section  
 298 2.3.1) calculated from a chosen insertion point (Figures 8,9). This allows providing the physician with  
 299 an automatically generated proposal and directs his attention towards those regions of the insertion  
 300 zone, which are best suited for an insertion.



301  
 302 **Figure 8.** Illustration of the concept of *pareto optimality* and trajectory selection explained for a two-  
 303 dimensional parameter space with the parameters insertion depth and distance to critical structures.  
 304 A point (e.g. p1) is called *pareto-optimal* if there is no other point that scores better in one  
 305 parameter without scoring worse in another. Point p2 is not *pareto-optimal* because p1 scores better  
 306 in both parameters. The line at the edge of the point cloud is called *pareto frontier* and includes all  
 307 *pareto-optimal* points. The rectangle marks all points that are in at least one parameter better suited  
 308 than the chosen insertion point. They form the so-called set of better points for a given insertion  
 309 point. The intersection between the *pareto frontier* and the set of better points contains all points  
 310 that are *pareto-optimal* and in all parameters better suited than the chosen insertion point.  
 311  
 312



313  
 314 **Figure 9.** Different types of trajectory selection assistance. (a) Transparent insertion zone (b) Set of  
 315 better points (green) which score in at least one parameter better than the chosen insertion point  
 316 (red). (c) *Pareto frontier* (blue) showing all *pareto-optimal* points, i.e. the set of points for which  
 317 there is no other point, which scores better in one parameter without scoring worse in another one.  
 318 Two selections are marked and the quantitative measures of the *soft constraints* distance to critical  
 319 structures (DTCS), trajectory length (TL) and insertion angle (IA) are provided. (d) Insertion points  
 320 lying both on the *pareto frontier* and in the set of better points (dark blue).  
 321

## 322 2.4 Slice-based correction

323 The slice-based planning offers the physician the possibility to plan or refine a trajectory on  
 324 reconstructed slices of the CT dataset (axial, sagittal, and coronal) or in an interactive three-

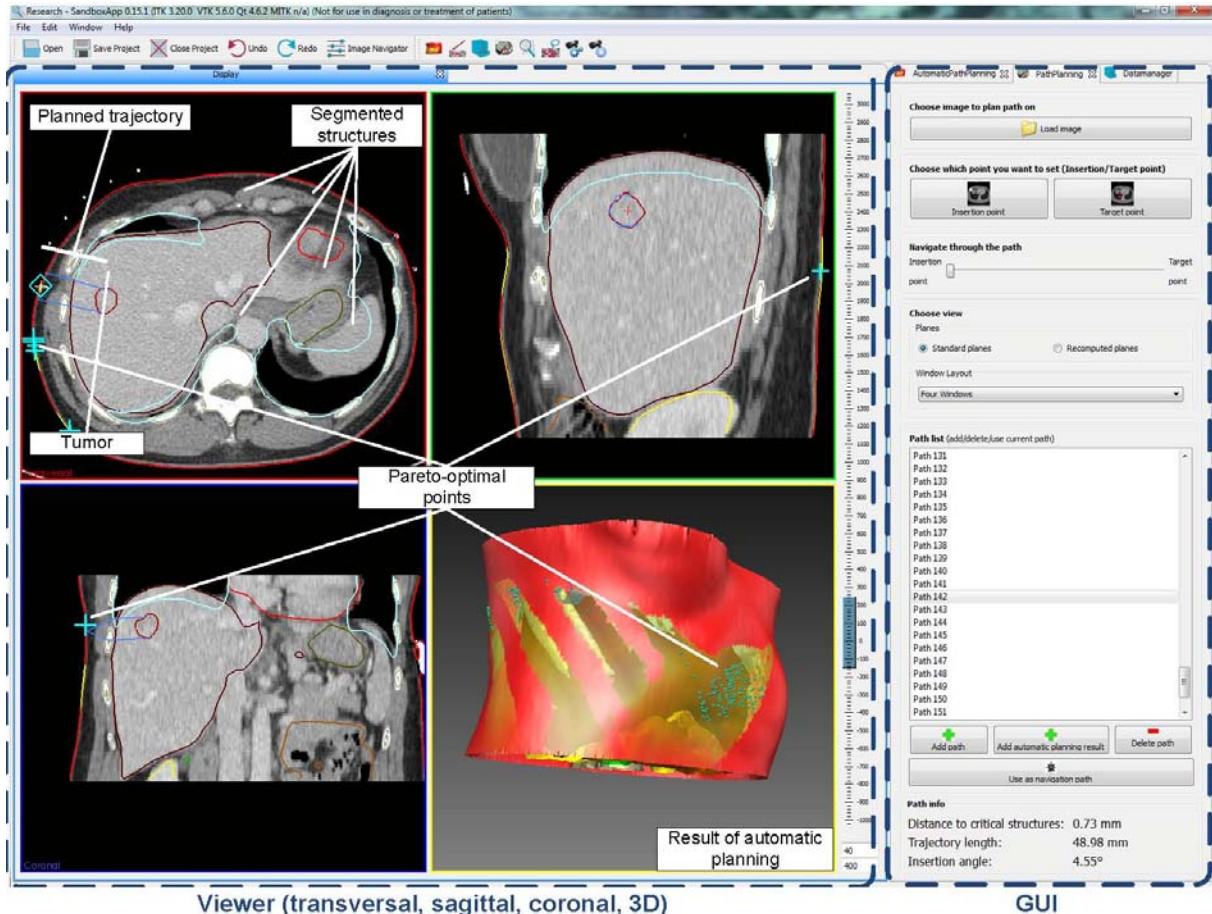


325 dimensional view. A point-and-click interface allows for easy interaction with the trajectory.

326 Additionally, there is a possibility to step through the planned trajectory and to reconstruct slices of

327 the data set, in which the trajectory is completely visible. All relevant structures can be visualized in

328 the two-dimensional slices and the three-dimensional view (Figure 10).



329 **Figure 10.** Trajectory planning interface realized within the Medical Imaging Interaction Toolkit

330 (MITK [19]). On the left side, the user can view the medical imaging data in multiple planar

331 reconstructions (transversal, sagittal, coronar) and also has interactive access to a 3D viewer which

332 presents e.g. 3D surface data. On the right, the graphical user interface (GUI) for the trajectory

333 planning provides tools for both automatic planning and manual trajectory refinement.

334

## 335 2.5 Evaluation

336 The evaluation of the proposed system for automatic trajectory planning was performed in a

337 retrospective study on n=10 clinical datasets which showed complications during the intervention

338 (e.g. pneumothorax, Table 1). The interventions were performed by different interventional

339 radiologists. For each intervention, a pre-interventional planning CT scan and multiple intra-

340 interventional control CT scans were acquired. To reduce the radiation exposure to the patient, the

341 control scan did only cover that region of the image showing the needle. In order to facilitate the  
 342 extraction of the chosen insertion point, the control scan was registered to the planning scan using a  
 343 point-based registration method [25]. Due to the retrospective nature of the study, the planning and  
 344 control scan were not always acquired in the same state of respiration. This affects the position and  
 345 size of the lungs in particular which have to be considered as critical structures. To compensate for  
 346 this and for breathing motion in general, we dilated the lung meshes by 12 mm, which represents the  
 347 mean lung motion in cranial-caudal direction (Seppenwoolde *et al.* [26]). Skin, liver, tumor, and  
 348 critical structures were segmented manually using the interactive segmentation framework of MITK  
 349 [20].

Case	Intervention	Complication	Needle type
1	Liver RFA	Pneumothorax	Single needle
2	Liver RFA	Pneumothorax	Single needle
3	Liver RFA	Pneumothorax	Starburst umbrella needle (Ø3cm)
4	Liver RFA	Pneumothorax	LeVeen umbrella needle (Ø2cm)
5	Liver RFA	Pneumothorax	LeVeen umbrella needle (Ø2cm)
6	Liver RFA	Pericardal effusion	Starburst umbrella needle (Ø3cm)
7	Liver RFA	Hematothorax	LeVeen umbrella needle (Ø2cm)
8	Liver RFA	Pneumothorax	Starburst umbrella needle (Ø3cm)
9	Drainage	Pneumothorax	Single needle
10	Drainage	Pneumothorax	Single needle

350 **Table 1.** Data sets used for the retrospective evaluation. The type of intervention, the type of  
 351 complication and the type of the needle used are shown. For the cases 9 and 10, the targets did not  
 352 lie inside the liver. Therefore, the liver specific constraints *safety margin around target* and *tangency*  
 353 were not applied.

354  
 355 The automatic planning was performed on all 10 datasets using a desktop computer (Intel® Core™i7,  
 356 2.93 GHz, 3.23 GB RAM, GeForce 8800GT, Windows XP, 32 bit).

357 For the technical evaluation, the runtime of each constraint and the remaining insertion zone after  
 358 application of the *hard constraints* were determined.

359 In the clinical evaluation, the result of the automated planning was retrospectively compared to the  
 360 clinically chosen trajectory to investigate, whether the *hard constraints* would have prohibited the  
 361 planned trajectory or if it would have been rated poorly by (one of) the *soft constraints*.

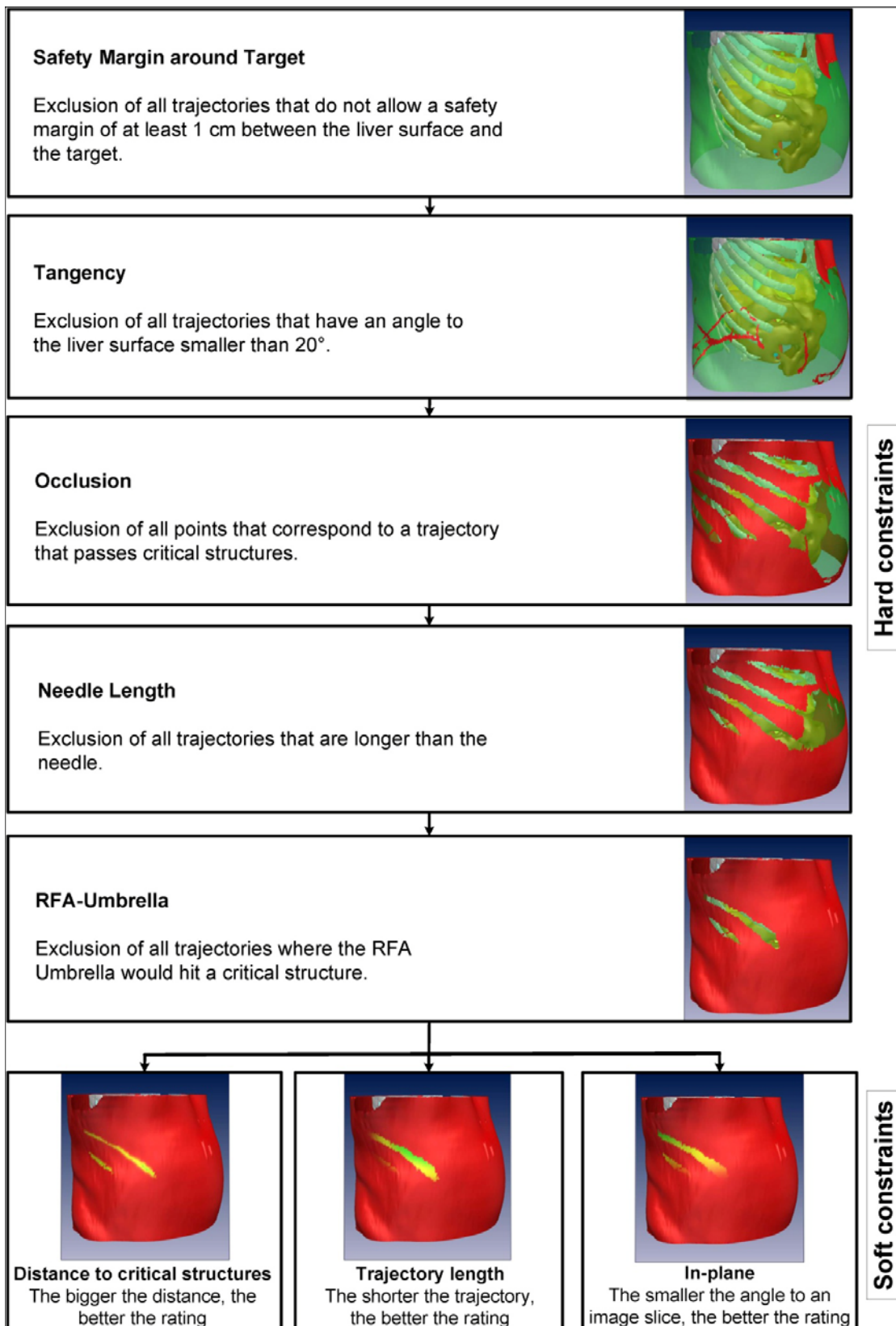
362 To assess the validity of the trajectories proposed by our system, we asked two interventional  
363 radiologists with experience in punctures and RFA (R1: more than 2500 punctures and more than 300  
364 RFAs, R2: more than 200 punctures and more than 50 RFAs) to use our software to select one point  
365 on the *pareto frontier* as potential insertion point for each of the ten cases of our retrospective data  
366 set. The experts were then asked to qualitatively compare the corresponding path with the actually  
367 chosen path by answering the following questions:

- 368 • Is the path proposed by the system a good proposal given the anatomy of the patient?
- 369 • Was the chosen insertion point a good choice?
- 370 • Which path would you prefer?

### 371 **3 Results**

372 Figure 11 illustrates the trajectory planning procedure performed for one of the ten patients for each  
373 step of the workflow and the resulting surface with transparent green insertion zone. Table 2 shows  
374 the mean execution times of the *hard constraints* and the *soft constraints*. Note that the execution of  
375 the *hard constraints* in the pipeline progressively eliminates points from the insertion zone and thus  
376 reduces the execution time for the constraints applied last in the pipeline. The execution time of the  
377 *hard constraints* ranged from  $0.02 \pm 0.00$  s for the *needle length constraint* to  $4.13 \pm 0.55$  s for the  
378 *RFA-umbrella constraint*. The *soft constraints* took  $0.02 \pm 0.00$  s (*insertion depth*),  $0.01 \pm 0.00$  s  
379 (*insertion angle*) and  $3.18 \pm 3.13$ s (*distance to critical structures*), respectively. The umbrella  
380 constraint could profit most from the execution in the constraints pipeline and could be executed  
381 about 38 s faster. The mean overall execution time of the entire automatic trajectory planning was  
382  $9.23 \pm 5.15$  s. Due to an improved GPU based implementation of the *occlusion constraint* its  
383 execution time could be decreased from  $24.39 \pm 3.10$  s for the approach as presented by Villard and  
384 Baegert to  $2.48 \pm 0.20$  s using similarly sized meshes, which is an improvement of 90%.

385



386 **Figure 11.** Trajectory planning workflow and resulting surfaces. For the *hard constraints*, the  
 387 insertion zone is shown transparently green. The result of the *soft constraints* is visualized with a  
 388 color gradient ranging from red (poor rating) to green (good rating).  
 389

	Constraint	Time (s)
	Safety margin around target (n=8)	1.27 ± 0.18
	Tangency (n=8)	0.04 ± 0.01
<b>HC</b>	Occlusion (n=10)	2.48 ± 0.20
	Needle Length (n=10)	0.02 ± 0.00
	Umbrella (n=6)	4.13 ± 5.29
	Distance to Critical Structures (n=10)	3.18 ± 3.13
<b>SC</b>	Insertion Depth (n=10)	0.02 ± 0.00
	Insertion angle (n=10)	0.01 ± 0.00

390 **Table 2.** Mean execution time in s for each *hard constraint* (HC) and *soft constraint* (SC) averaged  
391 over the specified number of datasets applicable for that constraint.

392  
393 Considering the remaining area for possible insertion points on the skin, the *occlusion constraint* is  
394 the most restrictive constraint, leaving only 18% of the patient's skin as insertion area. The *tangency*  
395 *constraint* in contrast leaves 93% for possible insertion (*safety margin around target*: 88%, *needle*  
396 *length*: 43%, *umbrella*: 5%).

Case	Complication	Expected result (organ)	Trajectory excluded?
1	Pneumothorax	Occlusion (lung)	No
2	Pneumothorax	Occlusion (lung)	No
3	Pneumothorax	Occlusion (lung)	Yes
4	Pneumothorax	Occlusion (lung)	Yes
5	Pneumothorax	Occlusion (lung)	Yes
6	Pericardial effusion	Umbrella (heart)	Yes
7	Hemothorax	Occlusion (lung)	Yes
8	Pneumothorax	Safety margin around target (liver)	Yes
9	Pneumothorax	Occlusion (lung)	No
10	Pneumothorax	Occlusion (lung)	No

397 **Table 3.** Performance of the *hard constraints*. For all 10 cases with complications, the *hard constraint*  
398 expected to exclude the chosen trajectory is given together with the actual exclusion result

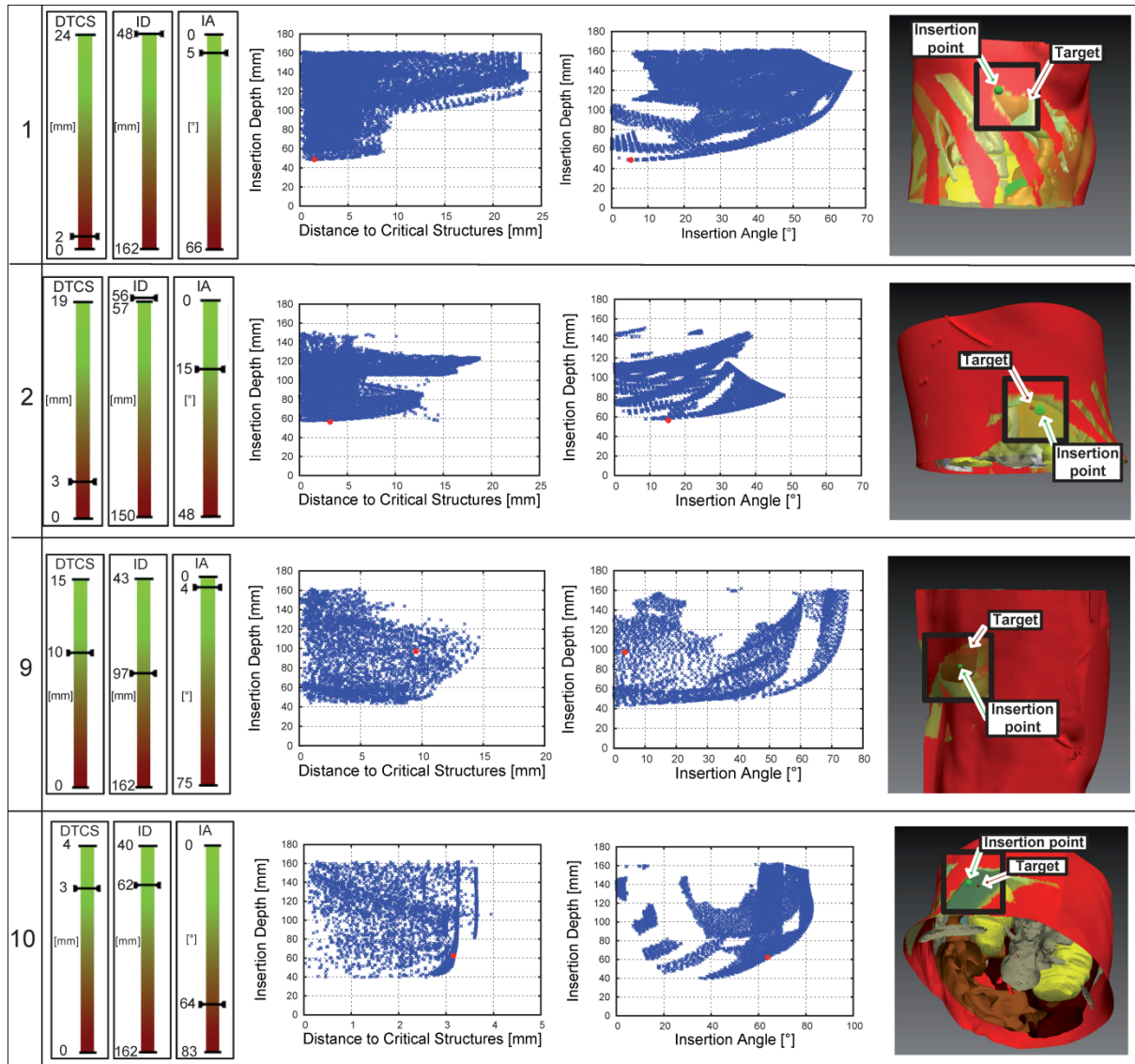
399  
400 As **Table 3** shows, the initially chosen insertion point was declared invalid by the planning system for  
401 six cases (3-8). For these cases, the correct *hard constraint* excluded the chosen trajectory. In case 3,  
402 for example, a pneumothorax occurred and the *occlusion constraint* declared the insertion point  
403 illegal with the lung being the restrictive critical structure. For the cases 1, 2, 9 and 10 the *hard*  
404 *constraints* did not exclude the chosen insertion points even though a pneumothorax occurred in  
405 those cases. The reader may be reminded that the respiratory motion causes an additional  
406 uncertainty for the planning in the position of the lungs. Additionally, due to the retrospective nature  
407 of this study, the organ positions in the planning and the control CT may differ. **Table 4** shows that in  
408 two of the four cases in which the chosen insertion point was valid, better points could be found for

409 which the rating of one or more *soft constraints* could be improved without worsening the remaining  
 410 *soft constraints*. For the two cases, where the automatic proposal could not find better points, the  
 411 physicians tended to choose a short insertion trajectory close to critical structures and almost in-  
 412 plane.

Case	Improvement possible?	Better points (% of insertion zone)			Insertion zone (cm <sup>2</sup> )
		DC	TL	IA	
1	No	89.0	0.03	1.9	293
2	No	62.3	0	32.9	220
9	Yes	12.6	52.0	5.2	81
10	Yes	33.1	9.3	50.1	91

414 **Table 4.** Quality of the chosen insertion point for the four data sets where the chosen insertion point  
 415 was declared valid by the *hard constraints*. The table shows if an improvement of the rating of one or  
 416 more *soft constraints* was possible without worsening the rating of the remaining constraints and  
 417 how many points (in percentage of the total number of points in the insertion zone) showed a better  
 418 scoring with respect to every single *soft constraints* (DC = distance to critical structures, TL =  
 419 trajectory length, IA = insertion angle). The size of the insertion zone given in cm<sup>2</sup>.

420  
 421 Figure 12 shows the chosen insertion point compared to all other points of the insertion zone  
 422 regarding the scores of each *soft constraint* for the four cases where the chosen trajectories were not  
 423 excluded by the *hard constraints*. In two of the four cases (1, 2), the physician chose trajectories  
 424 which were *pareto-optimal*. In both cases the path was chosen with a short *trajectory length*,  
 425 because these trajectories were technically easier to transfer to the patient. In contrast, many  
 426 insertion points with a bigger *distance to critical structures* could be found while only slightly  
 427 increasing the *insertion depth* or the *insertion angle*. In case 9 the trajectory was almost chosen *in-*  
 428 *plane* with a sufficiently big *distance to critical structures* while the resulting length of the trajectory  
 429 was rather long. Furthermore, the *insertion depth* could have been decreased without increasing the  
 430 *insertion angle* or decreasing the *distance to critical structures*, i.e., the chosen insertion point was  
 431 not *pareto-optimal*. In case 10, the trajectory length was considerably short, while the *distance to*  
 432 *critical structures* was very small and the angle to the transversal plane relatively big. The insertion  
 433 point was almost *pareto-optimal*, but the system identified several points with a smaller insertion  
 434 angle which decreases the uncertainties of an angulated needle insertion.



436  
 437 **Figure 12.** Results of the *soft constraints* for the four cases where the chosen insertion point was not  
 438 excluded by the *hard constraints*. (a) Score of the chosen insertion point visualized for each *soft*  
 439 *constraint* in a bar graph ranging from the worst to the best score. (b)+(c) Plots of the scores of all  
 440 points in the insertion zone and the chosen insertion point each shown for two of the *soft*  
 441 *constraints*. (d) Surface representation of the whole scene which shows the color-coded skin, critical  
 442 structures, and the target and insertion point chosen by the physician.

443 Figure 13 and Table 5 summarize the results of the quality assessment of the proposed trajectories.

444 R1 rated the trajectory he selected with the planning system better than the original path in all cases

445 and needed 3 minutes on average for the selection. However, for the cases 5 and 6 a suitable

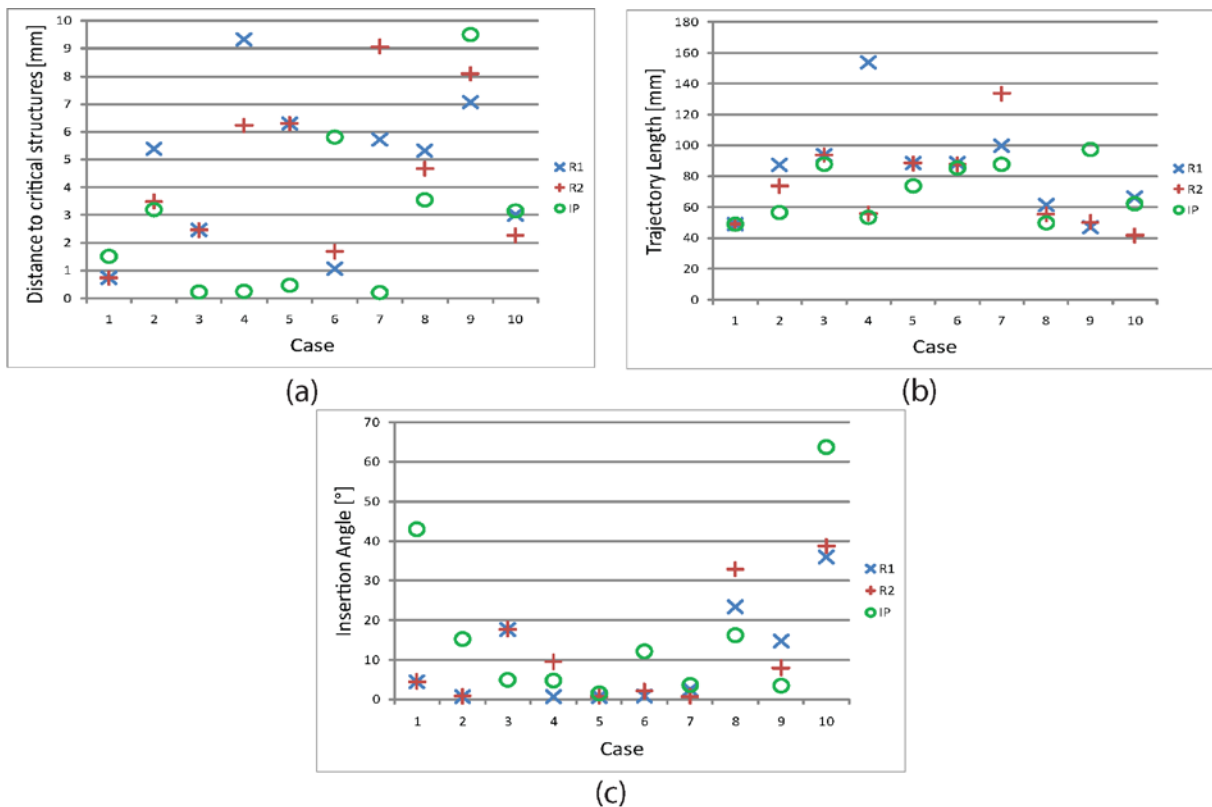
446 trajectory could only be found when not using the *umbrella constraint* because in these cases the

447 radiologist would not have fully deployed the spikes of the umbrella to cover the tumor, like it is

448 assumed by the constraint. R2 could find better trajectories in all cases but case 6 and also needed 3

449 minutes on average for the trajectory selection. For the cases 4, 5, 6 and 8 the *umbrella constraint*

450 was not used to select a trajectory. In some cases (4, 6, 9) several proposed trajectories were rated  
 451 poorly because they would hit the portal vein which was not included as a critical structure, because  
 452 no contrast enhanced CT scan was available. Our radiologists, however, would have used such an  
 453 additional scan for planning a safe trajectory. Furthermore two trajectories (case 8 and 10) were  
 454 rated technically good but difficult to perform. According to R1, the use of a navigation system such  
 455 as the one of Maier-Hein *et al.* [27] would be beneficial in these cases. Quantitatively, the trajectories  
 456 chosen by the radiologists were more distant to critical structures but longer compared to the  
 457 originally chosen insertion point.



458  
 459 **Figure 13.** Quality assessment of the *pareto-optimal* points proposed by the planning system. Two  
 460 interventional radiologists (R1, R2) each chose the subjectively best point from the *pareto frontier*.  
 461 The corresponding quantitative measures distance to critical structures (a), trajectory length (b), and  
 462 insertion angle (c) are shown for the selected points and the originally chosen insertion point (IP).  
 463 Note that the radiologists could only find suitable points when not using the umbrella constraint in  
 464 the cases 5, 6 (R1) and 4, 5, 6, 8 (R2).  
 465  
 466  
 467  
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472  
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474

Case	1		2		3		4		5		6		7		8		9		10	
	R1	R2	R1	R2	R1	R2	R1	R2	R1	R2	R1	R2	R1	R2	R1	R2	R1	R2	R1	R2
<b>better?</b>	+	+	+	+	+	+	+	+	+	+	-	+	+	+	+	+	+	+	+	+
<b>time (min)</b>	7	7	1	3	2	3	1	2	8	2	2	2	1	2	1	2	2	2	1	1
<b># points</b>	155		16		5		56		40		19		74		97		75		38	

475 **Table 5.** Selection of the insertion point from the *pareto frontier* and comparison with the original  
476 insertion point. The rows show whether the point that was selected by the interventional radiologist  
477 (R1 or R2) was better than the original point (better?) according to the radiologist himself. Time  
478 represents the duration of the manual part of the planning process based on the *pareto frontier*. #  
479 points ist the number of points on the *pareto frontier*.

480

## 481 **4 Discussion**

482 To our knowledge, we are the first to present a weight-independent approach for automatic  
483 trajectory planning in the abdomen. We could show in a retrospective study that our system is  
484 capable of preventing the user from choosing trajectories which are likely to lead to complications  
485 during an intervention. According to radiological experts, the trajectories proposed by the planning  
486 system are useful and valid for intervention. Only for one of the ten cases, the proposed path was  
487 rated poorly. Computation of a trajectory proposal based on an efficient implementation of the  
488 applied hard and *soft constraints* took about 9 seconds on average. The selection of an insertion path  
489 based on the proposal by the radiologist took 3 minutes on average.

490 The presented approach was designed to be extendable and can easily be adapted for other body  
491 parts in a straightforward manner. As there are currently no constraints as for needle and patient  
492 position, constraints ensuring that e.g. the inserted needle still fits in the gantry of the CT scanner or  
493 the patient is always supposed to be in supine position can be added to the automatic path planning  
494 workflow in a straightforward manner. In fact, integration of such constraints was also proposed by  
495 the radiologists that used the system. Similar approaches from Villard and Baegert [17] or Schumann  
496 *et al.*[18] also concentrate on the computation of suitable insertion trajectories, but still depend on  
497 an appropriate weighting of the different constraints to achieve the desired planning result. Utilizing  
498 a pareto-based optimization, our approach is able to propose insertion trajectories without needing

499 weights. Furthermore, the suitability of the approaches of Baegert *et al.* and Schumann *et al.* to  
500 support radiofrequency ablations or biopsies have not yet been evaluated in a clinical study.

501 As the state in the breathing cycle crucially affects both the poses and the dimensions of critical  
502 structures such as the lungs, it also has a high influence on the result of the planning. This could  
503 explain why only in six out of ten cases the chosen trajectories have been excluded by the system  
504 and that for two of the remaining cases no better trajectories could be found. We aimed to  
505 compensate for this by dilating the lung by the average lung movement. Incorporating a respiratory  
506 model for the lungs and the organs in the abdomen could possibly further improve the planning  
507 result. Furthermore, the respiratory states for intervention planning and needle insertion should be  
508 identical in future applications of the planning system. In this work we could not consider this issue  
509 due to the retrospective nature of the study. Nevertheless, the majority of the points of the insertion  
510 zone had a better rating by the *distance to critical structures constraint* compared to the chosen  
511 insertion point.

512 The use of surface meshes for the computation of the insertion zones leads to a dependency on the  
513 quality and the resolution of the mesh. The *tangency constraint* requires smooth meshes, as the  
514 angle to the liver surface is computed using the surface normals. Especially the *distance to critical*  
515 *structures constraint* and the newly proposed *RFA-umbrella constraint* strongly depend on the  
516 resolution of the meshes, because all mesh points of the critical structures are considered for  
517 computation of the planning result. Thus, the resolution of the mesh has to be carefully chosen to  
518 find a balance between runtime and planning accuracy. The *occlusion constraint*, directly using  
519 graphics rendering for computation, is also limited by the resolution of the used screen. We are  
520 currently working on a so-called off-screen rendering, which allows performing the rendering on  
521 arbitrary sized, virtual screens.

522 As a mesh representation of every critical structure is required for the trajectory planning, the fast  
523 segmentation of the liver, the critical structures, the skin and the target in the CT image, preferably in

524 an automatic way, remains an important problem. While the automatic segmentation of high  
525 contrast structures like bones and lungs can be done in an acceptable period of time, a precise  
526 segmentation of structures such as vessels, liver or kidneys can currently not be performed  
527 automatically in a reliable manner within less than one to a few hours, as they are usually performed  
528 with manual or semi-automatic segmentation methods. This is a problem if the planning CT is  
529 acquired within minutes before the intervention. Waiting for those segmentation methods to  
530 improve in efficiency, we can propose to use incomplete but fully automatic segmentation to provide  
531 a rough automatic planning which can then be refined using interactive methods such as the  
532 proposed slice-based correction tool. Furthermore, we are currently investigating a new visualization  
533 scheme for interactively refining the trajectory based on a GPU based volume visualization restricted  
534 to the possible insertion zones. For this purpose, we virtually remove the skin around the insertion  
535 point and thus provide a view along the trajectory which allows determining the quality of the path..

536 In further investigations, cases of needle insertions without complications should be considered to  
537 examine whether the system is able to confirm valid entry points. In an ongoing clinical study, we are  
538 currently investigating the quality of the planning results and the usability of the planning system  
539 together with interventional radiologists with experience in RFA. First results were presented in this  
540 work and showed that the system is able to propose safe trajectories. However, in four cases the  
541 *umbrella constraint*, which takes into account the shape of the RFA needle, had to be disabled in  
542 order for the radiologists to find a satisfactory path. This may be attributed to the fact that only a  
543 rigid shape of the RFA umbrella is considered in the planning process, while in clinical routine the  
544 deployment of the umbrella's spikes may vary to avoid hitting critical structures. Consideration of the  
545 portal vein for computing the planning proposal would further improve the result of the planning.

546 Because some proposed trajectories were rated safe and technically good but difficult to perform by  
547 the interventional radiologist due to the big insertion angle and trajectory length, the integration of  
548 the automatic trajectory planning in a navigation system such as proposed by Fichtinger *et al.* [28],  
549 Levy *et al.* [29] or Maier-Hein *et al.* [27] would be useful. These systems are potentially well-suited

550 for transferring relatively long trajectories to the patient, thus allowing giving high weight to the  
551 *distance to critical structures constraint* to prevent complications. This integration would also reduce  
552 the procedure time for navigated needle interventions where the trajectory planning turned out to  
553 be the most time consuming part [27]. Future work will also include embedding the system into the  
554 clinical IT workflow of a PACS system (e.g. the Chili system [30]) to simplify the transfer and the  
555 processing of the medical imaging data.

556 In conclusion, the proposed trajectory planning approach clearly shows benefits compared to the  
557 current state-of-the-art planning in clinical routine. In contrast to the conventional planning, which is  
558 performed manually on the imaging data, our approach utilizes the three-dimensional information  
559 provided by the imaging modality in order to account for critical structures, angle of penetration,  
560 needle length, and needle shape. Thus, the system is able to quickly detect unsafe paths and propose  
561 safe trajectories during the planning which may especially be helpful for radiologists at the beginning  
562 or during their interventional training. We believe that our approach could improve the clinical  
563 procedure of needle insertions such as radiofrequency ablations or biopsies regarding complication  
564 rate and intervention time.

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